Math 2471 – Spring 2010

Name

For full credit: use calculus to solve problems, circle answers, and **show all your work**.

Review for Test 3

1) Use the limit process to find the area under the curve of  $y = x^2 + 2$  on [2, 5].

2) I evaluated the integral  $\int_{-2}^{2} (x^3) dx =$  and

found the result to be zero. I double checked my work and found no errors; however, I know there is some area between the graph and the *x*axis. Please explain the result.

3) Evaluate the integral:  $\int_{2}^{5} (-3v+4)dv =$ 4) Determine the area under the curve  $y = (3-x)\sqrt{x}$  between x = 4 and x = 9.

5) Evaluate the integral without using calculus or your calculator:

6) Find the indefinite integral and check the result by differentiation of  $\int (t^2 - \sin t) dt$ .

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$$\int_{0}^{4} 3x dx =$$

7) Evaluate the integral: 
$$\int_{0}^{1} (x - x^2) dx = .$$
 8) Evaluate the integral:  $\int_{-1}^{1} (t^3 - 9t) dt$ 

9) Find the indefinite integral:

 $\int 5x * \sqrt[3]{1-x^2} dx =$ 

10) Evaluate the integral: 
$$\int_{0}^{\pi} (1 + \sin x) dx =$$

11) Find the equation of a line tangent to:  $y = \ln x^3$  at the point (1,0).

12) Find the derivative of:  $y = \ln(x\sqrt{x^2 - 1})$ .

13) If 
$$g(x) = (\ln x)^4$$
 then find  $g'(x) =$   
14) Find:  $\int \frac{x}{x^2 + 1} dx =$ 

15) Find the derivative of: 
$$y = \ln |\sin x|$$
.  
16) Evaluate:  $\int_{0}^{4} \frac{5}{3x+1} dx =$ 

17) Use logarithmic differentiation to find the derivative of:  $y = x^{x-1}$ 

18) Find the integral: 
$$\int 5^{-x} dx =$$

19) Solve the equation for *x*:  $\arcsin \sqrt{2x} = \arccos \sqrt{x}$ . 20) Solve the differential equation:  $\frac{dy}{dx} = x + 2$  21) Solve the differential equation:  $\frac{dy}{dx} = y + 2$  22) Find the **area** between  $f(x) = (x-1)^3$  and g(x) = x-1 on [0, 2].

23) Solve the differential equation:  $y' = \frac{5x}{y}$  24) Find the derivative of  $y = \ln |x|$ .

25) Find the integral: 
$$\int 5e^{5x} dx =$$
 26) If  $f(x) = \sqrt{x-4}$  then find  $f^{-1}(x) =$ 

27) Solve for *x*:  $e^{\ln x} = 4$ 28) Use logarithmic differentiation to find the derivative of:  $y = x^{2/x}$ 

29) Find the derivative of:  $f(x) = 2 \arcsin(x-1)$  30) Evaluate the integral:  $\frac{1}{6}$ 

$$\int_{0}^{1/6} \frac{3}{\sqrt{1-9x^2}} \, dx$$